Aboveground biomass relationships for beech (\textit{Fagus moesiaca} Cz.) trees in Vermio Mountain, Northern Greece, and generalised equations for \textit{Fagus} sp.

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(Received 5 July 2002; accepted 30 October 2002)

Abstract – Allometric equations describing tree size-shape relationships for beech (\textit{Fagus moesiaca} Cz.) in the Vermio Mountains of Northern Greece are presented. Diameter at breast height explained most of the variability in the dependent variables (total aboveground, stem, and branch biomass), while tree height was the second most important regressor in estimating foliage mass. Equations developed in USA and Europe for \textit{Fagus} spp. were also reported and validation with the field data indicated that the American regressions closely predicted total tree biomass for the study forest. In addition, the raw data were used to test a recent theoretical model and large deviations were found between theoretical and empirical values. Finally, generalised equations for \textit{Fagus} spp. were developed based on these data and several other published equations. Validation of the generalised equations indicated that accurate predictions may be obtained when these regressions are applied over a broad geographical area.

1. INTRODUCTION

Tree biomass plays a key role in sustainable management and in estimating the stocks of carbon (C) that forests contain. In addition to making estimates of C pools in forests, estimation of biomass is relevant for studying biogeochemical cycles, because the content of nutrient elements in forests is also related to the quantity of biomass present [16, 23, 31]. The most accurate way to determine values of wood biomass is to cut down the trees under investigation and perform appropriate measurements. However, destructively harvesting of forest biomass in sample plots is a time-consuming procedure and generates considerable uncertainty when the obtained results are extrapolated to larger areas [13]. Undoubtedly, the most common approach to obtain biomass estimates at stand level is through regression equations that are fitted to morphometric measurements taken from destructively sampling of individual trees. Subsequently, these regressions (also known as size allometry relationships) are used to estimate the biomass of sample plots within which the diameters and heights for all the

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trees have been measured. Researchers throughout the globe have developed a plethora of allometric equations for different species growing in a wide range of environmental conditions. However, aboveground tree biomass values vary with species, stand age, site quality, climate, and stocking density of stands [1, 4, 11]. Implementing allometric equations beyond the specific site and the diameter range for which they were developed is anticipated with scepticism. To circumvent this problem, Pastor et al. [21] developed generalised allometric equations for several north-American species and tests against field data indicated quite accurate predictions for some of them. Ketterings et al. [9] supported that aboveground biomass could be estimated without destructive measurements on sampled trees. They suggested that the parameters of allometric equations in biomass studies should depend on the average wood density, and on the exponent of the tree height-diameter relationship (see [9] for the detailed approach).

In a theoretical context, the allometric equations describing tree size-shape relationships are believed to be affected by the physiological requirements to conserve water and to support large loadings against the influence of gravity and/or wind forces [17]. With reference to foliage biomass, the underlying principle supports the idea that a unit of evaporating leaves is sustained by a unit of vascular pipes. This approach was developed by Shinozaki et al. [25] and is known as the "pipe model theory". Originally, it was thought that leaf mass was directly proportional to the basal area of the stems and branches, but several studies empirically demonstrated that the amount of foliage mass was strongly correlated with sapwood area e.g. [14]. McMahon and Kronauer [12] studied the scaling of tree height with respect to stem diameter using the stress and the elastic similarity models. Assuming a constant stem density, predictions about the relation between trunk mass and diameter are readily obtained [17]. Recently, West et al. [30] integrated the biomechanical and hydraulic principles of tree architecture, and developed a model which seems to predict quite accurately several structural plant variables (tree height and diameter, number of leaves, number of branches, etc.) in relation to plant body size (i.e. plant biomass). They supported that theoretical values obtained by the model are accurate enough to predict aboveground forest biomass. Parde [19] reviewed historical and methodological aspects of forest biomass studies and Cannell [4] compiled data on biomass production from studies conducted throughout the world.

The objective of this study is to develop biomass equations for beech (Fagus moesiaca Cz.) trees growing in Vermio Mountain, Northern Greece. Some preliminary results were presented by Zianis and Mencuccini [35]; in this paper, a more detailed analysis is attempted. The obtained equations are compared with the allometric equations for beech trees found in the literature and with theoretical model presented by West et al. [30]. Finally, an approach similar to that of Pastor et al. [21] was used in order to build and validate generalised allometric equations for Fagus genus. The obtained allometric relationships will be used to investigate the primary productivity of beech stands along an elevation gradient.

2. MATERIALS AND METHODS

2.1. Study area

The Vermio Mountain is situated in the central part of Northern Greece, about 80 km West of Thessaloniki, with a North-South orientation. The East-facing slopes are influenced by pluvial aerial masses originating from the Aegean Sea resulting in highly productive ecosystems in comparison to West-facing sites. The study forest (40° 32’ N, 21° 58’ E) is located on the Eastern slopes of Vermio Mountain, spanning from 380 to 2052 m above sea level and belongs to the Municipality of Naousa town. Several plant species (Pinus nigra Arn., Abies borsii-regis Mattf., Castanea sativa Miller., Ilex aquifolium L., Juniperus sp., Quercus sp., Salix sp., Populus sp., Platanus sp., Acer sp., Fraxinus sp., Buxus sempervirens L., Cornus sp., Prunus sp., Robus sp., etc.) could be found in this ecosystem. The climate of the forest can be classified as temperate Mediterranean with rainy winters and warm summers and the total annual rainfall is 1500 mm [27]. Minimum rainfall occurs during the July-August period, but the atmosphere is not totally dry due to the vicinity to archipelagos.

The Balkan region and particularly Northern Greece, is the contact zone of the European Beech (F. sylvatica subsp. sylvatica L.) and Oriental beech (F. sylvatica subsp. orientalis Lipsky). Strid and Tan [28] supported that F. sylvatica subsp. sylvatica and F. sylvatica subsp. orientalis are typical geographical races of F. sylvatica and several individuals have been recorded to be more or less intermediate between these subspecies. Such hybrids are referred to as F. sylvatica subsp. moesiaca Cz. (Moesian beech) with leaves characterised by 5–9 pairs of lateral veins and seeds often presenting somewhat spatulate basal cupule scales. However, Moesian beech is reported to be the prevalent species in Central and North-west Greece [6, 8, 24] and the morphological characteristics of the study trees resemble the Moesian type rather than the European form. Naturally regenerated, pure beech (Fagus moesiaca Cz.) stands occupy a total area of 2121 ha, stretching from 900 m to 1900 m and covering a range of various topographical conditions (see Tab. I). Due to the disturbed history of the forest (clearcut fellings during the 19th century and several fire events during World War Two), it is usual to meet cohorts within stands that belong to different age- and consequently size-classes.

2.2. Tree level data

Sixteen trees were harvested from the stands described in Table I for the parameterisation of the allometric equations and the diameter

<table>
<thead>
<tr>
<th>Stand ID</th>
<th>Elevation (m)</th>
<th>Aspect (Slope)</th>
<th>Density (trees/ha)</th>
<th>Basal area (m²/ha)</th>
<th>D range (cm)</th>
<th>Mean height (m)</th>
<th>Mean annual increment (m³/ha)</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>1030</td>
<td>N–NE (20%)</td>
<td>630</td>
<td>29.0</td>
<td>10–32</td>
<td>23.0</td>
<td>5.98</td>
</tr>
<tr>
<td>16b</td>
<td>1310</td>
<td>N–E (30%)</td>
<td>667</td>
<td>20.1</td>
<td>10–32</td>
<td>14.0</td>
<td>4.17</td>
</tr>
<tr>
<td>12a</td>
<td>1513</td>
<td>N–W (31%)</td>
<td>744</td>
<td>19.3</td>
<td>10–36</td>
<td>17.4</td>
<td>7.52</td>
</tr>
<tr>
<td>10a</td>
<td>1820</td>
<td>N–E (60%)</td>
<td>820</td>
<td>22.4</td>
<td>10–60</td>
<td>13.9</td>
<td>2.68</td>
</tr>
</tbody>
</table>
(D) range of the felled trees spanned from 5.19 to 40.6 cm so as to represent the diameter distribution reported in the forest management plan.

The following variables related to tree dimensions were recorded per sample tree: the diameter at 0.30 m above ground (DBh), the diameter at 1.30 m (D), the diameter at the base of the live crown (DC), the total height (H), the height to the base of the live crown (Hc), diameters (DBR), lengths (LBR) and positions of the branches on the stem. The tree bole was cut at 0.30 m and at 1 m intervals thereafter up to the base of the live crown (i.e. the point where the main stem bifurcated), and the part of the stem within the crown was separated from branches. After felling the tree, the stump was also removed. The leaves of each branch were collected and put into plastic bags. The stem sections (including bark), the stump, the branches and the leaves were transported to the laboratory and oven dried to constant weight at 80°C. Before felling, the horizontal projections of the 8 longest branches (excluding epicormics) were pointed down and the horizon-

2.3. Regression analysis

Foresters and ecologists have used different models for estimating forest biomass. Undoubtedly, the most commonly used mathematical model is the allometric equation corresponding to the following power form:

\[ Y = aX^b \]  

where a and b are the scaling coefficients that vary with the variables under investigation; Y is the total biomass or one of its components and X a tree dimension variable (i.e. D, D², D³H, DH, etc.).

Payandeh [22] further classified model (Eq. (1)) into two types: the “intrinsically linear” type which assumes a multiplicative error in raw data and the “intrinsically nonlinear” type with an additive random error. In the “intrinsically linear” model, the original data are log-transformed and the least square method is applied in order to estimate the parameters. In many cases, log-transformation of raw data results in homoscedasticity of the dependent variable Y, a prerequisite for the regression methods. However, even though the logarithmic equation is mathematically equivalent to equation (1), they are not identical in a statistical sense [34]. Using the logarithmic form of equation (1), produces a systematic underestimation of the dependent variable Y when converting the estimated InY back to the original untransformed scale Y. Although this inherent bias has long been recognised [7], concern of its potential impact on estimates of biomass is relatively recent [10, 15, 26]. Several procedures for correcting bias in logarithmic regression estimates have been advocated [2, 3, 26, 33].

Let \( \hat{Y}_c = e^{\hat{a}X + b \ln X} \) be the mean predicted value for a given X in arithmetic units. According to [2], an approximation of the corrected, unbiased estimate is

\[ \hat{Y}_c = e^{\hat{a}X + b \ln X + CF} \]

where \( CF = \frac{SEE^2}{2} \) is the correction factor and \( SEE = \sqrt{\frac{\sum (\ln Y - \hat{Y})^2}{n - p}} \) is the standard error of the estimate of the regression; n and p denote the number of the observations and the fitted parameters, respectively.

Madgwick and Satoo [11] found from intensive sampled actual weights that with some corrections, values tend to be underestimated, and they suggested that, as the bias from re-transformation is generally small compared to the overall variation in the estimate of biomass, the correction factor be ignored. In addition, Beauchamp and Olson [3] reported that data on stem biomass of Liriodendron tulipifera L. showed small bias (< 1%) in the predicted dry weight obtained from the biased (uncorrected) estimate. For the purposes of the present study, a and b values are reported for the biased regression in conjunction with the correction factor CF as given by Sprugel [26].

Yandle and Wiant [33] reported that the bias \[ B = Y_c - Y, \] as a percent of the unbiased estimate equals to

\[ \text{Percent bias} = \frac{(e^{CF} - 1)\hat{Y}}{\hat{Y}} \times 100 \]  

and is constant over the range of X values. Wiant and Harner [32] suggested that it is informative to express the standard error of \( \hat{Y}_c \) for a given X as a percent of \( \hat{Y}_c \). This becomes

\[ \text{Percent standard error} = (e^{CF} - 1)^{1/2} \times 100 \]  

which is also constant over the range X values.

Usually, the validity of the relationship is tested by the coefficient of determination of the logarithmic regression, \( R^2 \), and \( SEE \) is computed for the entire dataset of the transformed data. However, high values of \( R^2 \) and small values of SEE (typically obtained in allometric studies) do not guarantee precision of the estimate, when values are back transformed to the linear scale. Thus, it is not unusual that, for a specific diameter, the predicted biomass \( \hat{Y} \) deviates by a relative amount of 90% from the corresponding observed value.

On the other hand, the general linear regression procedure does not apply to the “intrinsically nonlinear” model and iterative procedures are required for estimating the allometric parameters. Payandeh [22] reviewed and compared the log-transformed linear model with the simple nonlinear form and pointed out that the latter model resulted in better fit for two datasets of Betula alleghaniensis Britton and Acer saccharum Marsh.

Another basic point about allometric studies is that researchers rarely validate the obtained relationships with data other than the ones that were used in regression analysis. Madgwick [10] pointed out that if models are to be used for prediction purposes, they should be evaluated with new data. Moreover, it must be emphasised that allometric relationships are only valid over a certain X interval of the independent variables, and extrapolation to either higher or lower values may result in large deviations between real and predicted values.

Parresol [20] reported several statistics for evaluating goodness-of-fit and for comparing alternative biomass models. The mean percentage difference (MPD) between the predictions and the raw data was used to assess the performance of different models. This statistic gives the average deviation of the regression, relative to the raw data, and assesses the variability of the fitted equation. MPD is calculated as the average of differences between observed and predicted values divided by the observed [17, 22].

2.4. Generalised equations

Apart from estimating biomass values at stand level, predictions at landscape scale are also needed, especially for C related studies. Since it would be unrealistic to develop allometric equations for each stand found in a region, Pastor et al. [21] built generalised equations based on published allometric relationships. Quite a similar approach is presented in this paper in order to obtain generalised equations for beech trees, which were derived from American and Europeans studies (Tab. II).

The D range of each dataset was divided into four classes and the mean value of each class was used to derive the total aboveground biomass (MT) predictions from the original equations. These MT-D pairs (28 in total) were log-transformed and a generalised equation for aboveground dry biomass of beech trees was subsequently obtained.
Table II. Published equations for beech trees of the form $Y = aX^b$ used to develop generalised allometric relationships for aboveground dry biomass.

<table>
<thead>
<tr>
<th>Species</th>
<th>$a$</th>
<th>$b$</th>
<th>$R^2$</th>
<th>$D$ (cm)</th>
<th>$N^*$</th>
<th>Region</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fagus grandifolia</td>
<td>0.2013</td>
<td>2.2988</td>
<td>n/a</td>
<td>3–66</td>
<td>29</td>
<td>USA, Maine</td>
<td>[29]</td>
</tr>
<tr>
<td>Fagus grandifolia</td>
<td>0.1958</td>
<td>2.2538</td>
<td>0.99</td>
<td>2–29</td>
<td>46</td>
<td>USA, New Brunswick</td>
<td>[29]</td>
</tr>
<tr>
<td>Fagus grandifolia</td>
<td>0.1957</td>
<td>2.3916</td>
<td>0.99</td>
<td>1–60</td>
<td>14</td>
<td>USA, New Hampshire</td>
<td>[29]</td>
</tr>
<tr>
<td>Fagus grandifolia</td>
<td>0.0842</td>
<td>2.5715</td>
<td>0.97</td>
<td>5–50</td>
<td>56</td>
<td>USA, West Virginia</td>
<td>[29]</td>
</tr>
<tr>
<td>Fagus sylvatica L.</td>
<td>0.0798</td>
<td>2.601</td>
<td>0.99</td>
<td>2–32</td>
<td>32</td>
<td>EU, Netherlands Centre</td>
<td>[1]</td>
</tr>
<tr>
<td>Fagus sylvatica L.</td>
<td>0.1326</td>
<td>2.4323</td>
<td>0.99</td>
<td>4–35</td>
<td>7</td>
<td>EU, Spain North</td>
<td>[23]</td>
</tr>
<tr>
<td>Fagus moesiaca Cz.</td>
<td>0.2511</td>
<td>2.3485</td>
<td>0.99</td>
<td>5–41</td>
<td>16</td>
<td>EU, Greece North</td>
<td>This study</td>
</tr>
</tbody>
</table>

* Number of harvested trees.

Table III. Regression equations of the form $Y = \ln a + bX$. The standard errors of the estimates (s.e.) are significant at the 5%-level; $R^2$, SEE, CF, and SSE denote respectively the coefficient of determination, the standard error of the estimate for 14 degrees of freedom, the correction factor and the sum of squares for error in arithmetic units. Percent bias and Percent s.e. were computed with equation (2) and equation (3) respectively. The number of sampled trees was 16.

<table>
<thead>
<tr>
<th>$Y$</th>
<th>$X$</th>
<th>$\ln a$</th>
<th>$b$</th>
<th>$R^2$</th>
<th>s.e. ($a$)</th>
<th>s.e. ($b$)</th>
<th>$SEE$</th>
<th>$CF$</th>
<th>Percent bias</th>
<th>Percent s.e.</th>
<th>SSE</th>
<th>MPD (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>lnMT</td>
<td>lnD</td>
<td>-1.3816</td>
<td>2.3485</td>
<td>0.99</td>
<td>0.2080</td>
<td>0.0724</td>
<td>0.1841</td>
<td>1.0171</td>
<td>1.6819</td>
<td>18.5762</td>
<td>139617.36</td>
<td>14</td>
</tr>
<tr>
<td>lnMS</td>
<td>lnD</td>
<td>-1.6015</td>
<td>2.3427</td>
<td>0.98</td>
<td>0.2358</td>
<td>0.0821</td>
<td>0.2088</td>
<td>1.0220</td>
<td>2.1563</td>
<td>21.1099</td>
<td>91511.54</td>
<td>16.06</td>
</tr>
<tr>
<td>lnMT</td>
<td>lnD</td>
<td>-5.2898</td>
<td>2.9353</td>
<td>0.97</td>
<td>0.3686</td>
<td>0.1284</td>
<td>0.3264</td>
<td>1.0547</td>
<td>5.1902</td>
<td>33.5387</td>
<td>149235.35</td>
<td>25.38</td>
</tr>
<tr>
<td>lnMB</td>
<td>lnD</td>
<td>-6.3807</td>
<td>3.1037</td>
<td>0.95</td>
<td>0.5573</td>
<td>0.1941</td>
<td>0.4936</td>
<td>1.1295</td>
<td>11.4707</td>
<td>52.5287</td>
<td>13605.48</td>
<td>37.82</td>
</tr>
<tr>
<td>lnMB</td>
<td>lnD</td>
<td>-5.9523</td>
<td>2.7501</td>
<td>0.75</td>
<td>1.2032</td>
<td>0.4191</td>
<td>1.0657</td>
<td>1.7645</td>
<td>43.3271</td>
<td>145.379</td>
<td>12658.01</td>
<td>86.89</td>
</tr>
<tr>
<td>lnMT</td>
<td>lnD</td>
<td>-4.1814</td>
<td>1.6645</td>
<td>0.90</td>
<td>0.4362</td>
<td>0.1519</td>
<td>0.3863</td>
<td>1.0774</td>
<td>7.19</td>
<td>40.1176</td>
<td>10.94</td>
<td>39.92</td>
</tr>
<tr>
<td>lnMT</td>
<td>lnD</td>
<td>-5.5168</td>
<td>1.9979</td>
<td>0.87</td>
<td>0.5970</td>
<td>0.2079</td>
<td>0.5287</td>
<td>1.15</td>
<td>13.0474</td>
<td>56.7997</td>
<td>8.67</td>
<td>40.26</td>
</tr>
<tr>
<td>lnMB</td>
<td>lnD</td>
<td>-3.5789</td>
<td>0.9021</td>
<td>0.40</td>
<td>0.8420</td>
<td>0.2933</td>
<td>0.7458</td>
<td>1.3206</td>
<td>24.2792</td>
<td>86.2607</td>
<td>3.25</td>
<td>59.36</td>
</tr>
<tr>
<td>lnMB</td>
<td>lnD</td>
<td>-1.7716</td>
<td>1.0730</td>
<td>0.78</td>
<td>0.4398</td>
<td>0.1532</td>
<td>0.3895</td>
<td>1.0788</td>
<td>7.3068</td>
<td>40.4809</td>
<td>35.3</td>
<td>27.86</td>
</tr>
<tr>
<td>lnMB</td>
<td>lnD</td>
<td>-4.0543</td>
<td>2.2116</td>
<td>0.87</td>
<td>0.6683</td>
<td>0.2328</td>
<td>0.5918</td>
<td>1.1914</td>
<td>16.0686</td>
<td>64.7719</td>
<td>1328.3</td>
<td>44.47</td>
</tr>
<tr>
<td>lnMB</td>
<td>lnD</td>
<td>-4.1293</td>
<td>2.6741</td>
<td>0.96</td>
<td>0.4038</td>
<td>0.1407</td>
<td>0.3576</td>
<td>1.0660</td>
<td>6.1942</td>
<td>36.9358</td>
<td>12433.56</td>
<td>34.6</td>
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<tr>
<td>lnH</td>
<td>lnD</td>
<td>1.4192</td>
<td>0.5358</td>
<td>0.89</td>
<td>0.1459</td>
<td>0.0508</td>
<td>0.1292</td>
<td>1.0083</td>
<td>0.8315</td>
<td>12.9768</td>
<td>112.13</td>
<td>9.5</td>
</tr>
<tr>
<td>lnH</td>
<td>lnD</td>
<td>1.2238</td>
<td>0.4677</td>
<td>0.75</td>
<td>0.2052</td>
<td>0.0715</td>
<td>0.1818</td>
<td>1.0166</td>
<td>1.639</td>
<td>18.33</td>
<td>86.75</td>
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</tr>
<tr>
<td>lnH</td>
<td>D</td>
<td>1.1544</td>
<td>0.0504</td>
<td>0.91</td>
<td>0.0949</td>
<td>0.0042</td>
<td>0.1869</td>
<td>1.0176</td>
<td>1.7328</td>
<td>18.862</td>
<td>121.69</td>
<td>14.37</td>
</tr>
</tbody>
</table>

$MT$: total aboveground biomass, $MC$: stem mass, $M_{BT}$: branch mass (including epicormics), $M_{BC}$: branch mass in crown, $M_{GB}$: mass of epicormic branches, $M_{FC}$: foliage mass in crown, $M_{TF}$: foliage mass of epicormics branches, $M_{FT} = M_{FC} + M_{FE}$, $MPD$: stump mass, $MC$: the mass of the stem within the crown, $M_{CW} = M_{BC} + M_{CS}$. For $D$, $DC$, and $H$ see Section 2.2. Biomass is expressed in kg, diameter in cm, and height in m.

3. RESULTS

3.1. Allometric equations

Scatter plots of the data indicated that biomass values for different tree compartments, as well as for $H$, $H_C$, $D_C$ and $P_a$, were non-linearly related to $D$. Subsequently, the raw values were transformed using the Napierian logarithmic function and the least squares method was applied to estimate the parameters of the models. The results are presented in Table III and surprisingly strong relationships were obtained in almost all cases.

In one case however, the mass of the leaves of the epicormics branches ($M_{FE}$) was not highly correlated to $D$ as indicated by the $R^2$ of the log-transformed data. The MPD for $M_{BE}$ was about 87% but $D$ explained 75% of the variability of the biomass of epicormic branches. Stronger relationships are reported for total foliage biomass ($M_{FT}$) and for the mass of leaves found in the canopy ($M_{FC}$). In the following equations, $H$ is introduced as the second independent variable and slightly better predictions for $M_{FT}$ and $M_{FC}$ were obtained than with the allometric equation including only $D$:

$$M_{FT} = 0.0001997(0.000012)D^2H + 0.331(0.227), \quad R^2 = 0.9493$$

(4)

and

$$M_{FC} = 0.0001663(0.000013)D^2H + 0.224(0.243), \quad R^2 = 0.919.$$  

(5)

The standard errors of the estimates are presented in the parentheses; in both equations the slopes were statistically different from zero but the 95% range of the intercepts included this value.

However, the addition of $H$ for predicting the biomass of other tree compartments did not substantially contribute to the
increase of $R^2$ or to the decrease of SEE. The height of the stem was also closely related to $D$ according to $H_S = 3.4001D^{0.4677}$ (as transformed from the logarithmic equation in Tab. III).

Stump mass generally increased with increasing $D$ (Tab. III) or $DB$ (Fig. 1) but a large variability occurred, which resulted in a rather low $R^2$.

Subsequently, the stump shape was approximated as a cylinder with diameter and height equal to $DB$ and 0.3 m respectively, and the standard volume formula was used for predicting $MSP$; however, this approach did not significantly decrease the SEE (data not shown).

A highly exponential relationship between $\ln DC$ and $D$ was obtained (Tab. III) which, after transformation of the coefficients to arithmetic scale reads as

$$Dc = 3.172e^{0.0504D} \quad (6)$$

where $e$ is the base of Napierian logarithms. The horizontal projection area of crown ($Pa$), was also non-linearly related to $D$ and the empirical relationship was

$$Pa = 1.2830(0.1121)\ln D - 0.9004(0.321) \quad (7a)$$

with $R^2 = 0.9034$, and standard errors in parentheses.

The percent bias was computed according to equation (2) and resulted in a rather low estimate of 3.98%. Thus, no procedures were adopted in order to eliminate the inherent bias and the antilog of the logarithmic predicted values were used to derive the power function

$$Pa = 0.4064D^{1.2830} \quad (7b)$$

with sum of squared errors, $SSE = 1021.99$ (in linear scale); the projection area was measured in m² and $D$ in cm.

Larger values of percent bias (43.43%) were obtained for the equation that relates the biomass of epicormics branches ($MBE$) to $D$; however, the $SSE$ of the biased and corrected equations was 12.658 and 12.657 respectively (in linear scale), indicating that unbiased predictions do not significantly reduce the residual error.

Finally, the pooled data for the branches were used to derive the following relationship between branch biomass $M_{BR}$ and branch diameter $DBR$:

$$\ln M_{BR} = 3.415(0.062) + 2.818(0.056) \ln DBR \quad (8)$$

with $R^2 = 0.889$, $SEE = 0.6871$, and standard errors of parameters in parentheses.

The equations developed so far were assumed to comply with the “intrinsically linear” model and the least squares method was applied to log-transformed data in order to derive empirical values for the parameters of the allometric relationships. However, if one assumes an additive error term in the original data, then predictions should be based on nonlinear functions. The underlying model requires iterative procedures [22] for parameter estimation. Nonlinear equations were developed for the major tree biomass compartments (Tab. IV).

### 3.2. Generalised equations

A generalised equation for the aboveground biomass was developed, based on published allometric equations (see Tab. II) and the obtained relationship in logarithmic form is following:

$$\ln M_T = 2.45(0.055)\ln D - 2.004(0.168) \quad (9)$$

with $R^2 = 0.987$, $SEE = 0.1876$, standard errors in parentheses; (see Fig. 2).

Raw data for $M_T$-$D$ pairs reported by Santa Regina and Tarazona [23] were used, in conjunction with the new dataset reported in this study, to validate the generalised equation. To avoid confounding results, the Spanish and Greek equations

### Table IV. Regression equations of the form $Y = aX^b$. Symbols as in Table III.

<table>
<thead>
<tr>
<th>$Y$</th>
<th>$X$</th>
<th>$a$</th>
<th>$b$</th>
<th>$R^2$</th>
<th>s.e. ($a$)</th>
<th>s.e. ($b$)</th>
<th>$SSE$</th>
<th>$MPD$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$MT$</td>
<td>$D$</td>
<td>0.9402</td>
<td>1.9643</td>
<td>0.97</td>
<td>0.4897</td>
<td>0.1474</td>
<td>87058.6</td>
<td>25.77</td>
</tr>
<tr>
<td>$Ms$</td>
<td>$D$</td>
<td>0.7568</td>
<td>1.9536</td>
<td>0.97</td>
<td>0.4007</td>
<td>0.1498</td>
<td>54623.8</td>
<td>25.88</td>
</tr>
<tr>
<td>$MBT$</td>
<td>$D$</td>
<td>0.1097</td>
<td>2.0545</td>
<td>0.91</td>
<td>0.116</td>
<td>0.2985</td>
<td>8467.7</td>
<td>45.43</td>
</tr>
<tr>
<td>$MFT$</td>
<td>$D$</td>
<td>0.0057</td>
<td>1.9836</td>
<td>0.96</td>
<td>0.0035</td>
<td>0.1758</td>
<td>5.23</td>
<td>39.92</td>
</tr>
</tbody>
</table>

Figure 1. Stump biomass $M_{SP}$ in relation to $DB$. The slope is statistically different from one.
were excluded for the development of the new generalised equation which takes the form:

$$\ln M_T = 2.456(0.05)\ln D - 2.073(0.156)$$  \hspace{1cm} (10)

with $R^2 = 0.992$, $SEE = 0.1551$, (standard errors in parentheses).

The new generalised equation (10) very closely predicted biomass values for the Spanish dataset and there was virtually no difference between estimations made by the original and by the generalised regression (Fig. 3a). On contrary, the generalised equation did not accurately fit the data collected from the Greek stand (Fig. 3b).

For the original equation $MPD = 13.54\%$, while the generalised regression yielded a $MPD$ of 31.17\%. In addition, the pooled data from the two datasets were used to validate the

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**Figure 2.** Generalised equation (9) and original equations for aboveground biomass $M_T$.

**Figure 3.** Predicted values for aboveground biomass ($M_T$) from the generalised equation (10) and from original equations for the (a) Spanish and (b) Greek datasets.
generalised relationship. A MPD of 23.82%, which denotes a rather accurate estimate, considering that no adjustments were introduced to take into account the different anatomical and morphological characteristics of the harvested trees (stand structure, wood density, tree age, tree height, etc.). Generalised equations for other tree compartments (stem, branches, foliage) were also developed for Fagus spp. and the results are presented in Figure 4 (see also Tab. V).
To assess the variability of the generalised equations relative to the original regressions, Pastor et al. [21] reported three statistics. In this paper, the MPD between the predictions made by the generalised and the original equations was calculated for different biomass components and presented in Table V.

### 3.3. Comparison between equations

The American regression (developed in New Hampshire) better predicted the Greek raw $M_T$ values (Fig. 5), than the Spanish and Dutch equations which deviated by a large amount in relation to the raw data, constantly underestimating the aboveground dry biomass values.

This trend was also evident for the stem and foliage biomass, but the most accurate prediction for branch mass was obtained with the Dutch regression. In addition, it is illustrated in Figure 5 that the equation developed from beech trees harvested in Netherlands accurately predicted $M_T$ from the Spanish dataset.

We also explored the applicability of a new theoretical model at the stand and regional scale, by comparing the predictions against the Spanish and the Greek datasets. According to West et al. [30], the theoretical exponent ($b$) in the power function (Eq. (1)) equals 2.67 for the aboveground biomass, independently of species or site under investigation, but no estimation is given for the parameter $a$. However, Chambers et al. [5] reported that $a$ is ca. 0.1002, and this value was used to derive theoretical predictions. The MPD between the theoretical and raw values for the Greek dataset was 23.65% with the highest value amounted to 58% for the largest tree ($D = 41.45$ cm) and to 40% for the smallest tree ($D = 5.39$ cm). The MPD was larger for the Spanish data (49%) and the highest value was equal to 80% for a tree with a diameter equal to 34.5 cm.

### 4. DISCUSSION

#### 4.1. Allometric relationships

Diameter at breast height explained much of the variability in biomass values of different tree compartments. Adding $H$ as a second variable, improved predictions for foliage biomass were obtained, in accordance with Bartelink [1]. However, tree height did not substantially decrease the SSE for the regressions of total, stem, and branch biomass. The high correlation between $D$ and $H$ may explain the low gains in predictions when the latter variable is included in allometric models (multicolinearity). Mcmahon and Kronauer [12] examined the scaling of tree height based on stress and elastic similarity models and Niklas [17] reported that, for very old dicot trees, $H \propto D^{0.474}$ implying that mature trees taper so as to maintain a constant elasticity throughout the tree. In this study, the 95% confidence intervals for the reduce major axis scaling exponent of $H$ against $D$ are 0.45–0.66 and indicate that wind-pressure dynamic loadings most likely affect the size-shape relationship of the study trees. Strong scaling relationships were also found between different tree dimensions (i.e. $Pa$, $Dc$, $H_g$) and $D$ as well as between branch biomass and branch diameter. It

### Table V. Generalised equations for different tree compartments for *Fagus* spp. derived from the sources presented in Table II. MPD denotes the average deviation of the generalised predictions in relation to the original equations.

<table>
<thead>
<tr>
<th>Compartment</th>
<th>$a$</th>
<th>$b$</th>
<th>$D$ range (cm)</th>
<th>$R^2$</th>
<th>MPD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>0.1348</td>
<td>2.4500</td>
<td>1–66</td>
<td>0.99</td>
<td>14.86%</td>
</tr>
<tr>
<td>Stem</td>
<td>0.1321</td>
<td>2.3594</td>
<td>1–66</td>
<td>0.99</td>
<td>12.67%</td>
</tr>
<tr>
<td>Branches</td>
<td>0.0219</td>
<td>2.4208</td>
<td>1–66</td>
<td>0.77</td>
<td>58.11%</td>
</tr>
<tr>
<td>Foliage</td>
<td>0.0188</td>
<td>1.8169</td>
<td>1–66</td>
<td>0.86</td>
<td>32.29%</td>
</tr>
</tbody>
</table>
is obvious that stump biomass is not so tightly related to either $D$ or $D_B$ as indicated by the $R^2$ values (Tab. III and Fig. 1). An explanation could be that the sample trees were located at sites with different slopes, which in turn may influence the shape – butteressness – of the lowest part of the stem. This variability in shape could not be captured by $D_B$ alone and it is speculated that other variables might be more useful in predicting stump biomass. However, the information collected from the harvested trees could not be used to thoroughly test this hypothesis; compared to total tree biomass, stump mass is a very small proportion and any deviations from real values would be insignificant when extrapolated to stand scale. In statistical terms, the highest inherent bias recorded in the dependent variables after log-transformation was for the biomass of epicormic branches: the percentage bias value was equal to 43.32% (Tab. III). Applying the appropriate formula to eliminate this bias, the $SSE$ was insignificantly reduced (from 12658.01 to 12657.9); this observation was also true for other tree compartments, in accordance with [3] and [11]. When nonlinear models (Tab. IV) were compared with log-transformed regressions (Tab. III) it appeared that the former fitted the field data better than the latter as implied by the $SSE$. However, in terms of $MPD$, the linear models appeared to deviate less than the simple power functions, for total aboveground, stem and branch biomass.

Since data were pooled from stands with different structural and topographical characteristics (Tab. I), one could expect that quite accurate estimates may be obtained if the presented equations are to be applied throughout the study forest. Thus, the established relationships may be quite useful for the sustainable management of the investigated forest since no model existed so far for biomass estimations and the planning activity was totally based on the experience of foresters rather than on statistically sound methods.

### 4.2. Generalised equations

Aboveground biomass was estimated very accurately by generalised equations in the case of Spanish stand (Fig. 3a). On the other hand, the mean percentage difference (31.17%) between the generalised equation and the Greek dataset was relatively high (Fig. 3b), but within the range (10–35%) reported for published regressions developed from field data (Pastor et al. [21]). Mean variability between predicted and pooled stem biomass data was less than 27% (Fig. 4a), and was about 40% for the pooled branch biomass data (Fig. 4b). Generalised regression for foliage mass failed to predict the Greek data correctly ($MPD = 123\%$) but reasonably approximated the values of the Spanish stand ($MPD = 20\%$). The large deviation for the Greek dataset may be explained by the fact that foliage mass is strongly related to sapwood area rather than to $D$, as documented in several studies [1, 12]. For the pooled dataset, $MPD = 92\%$ (Fig. 4c).

The generalised regressions accounted for more than 98% of the variation in the values predicted by the original published equations, for total and stem biomass (Tab. V). The mean percentage difference between values obtained by generalised equations and those predicted by individual regressions for branch and foliage biomass was 58% and 32% respectively (Tab. V). Pastor et al. [21] reported similar percentage difference values for branch mass, and assigned this large deviation to the difficulties in separating stem and branches in broadleaved trees. Differences in silvicultural treatments, or site productivity or stand age may also explain the obtained values.

In general, it is clear that inaccurate predictions may be obtained from generalised equations when applied to any particular stand. However, over- and under-estimations from generalised predictions may cancel out when these are applied to large geographical areas, but more data are needed to robustly test this hypothesis. This method might prove useful in estimating dry biomass values at a national level with minimum cost, since it appears to provide a good balance between accuracy of predictions and low input requirements. It is obvious that this method can also be applied for other tree variables or life forms.

### 4.3. Comparison between equations

The sustained total aboveground biomass per tree is greater for the study forest in Vermio mountain than for the Dutch or the Spanish forests, as implied by the coefficients of the allometric equations in Table II. Larger biomass values in Vermio mountain in comparison to the Dutch study may be explained by the fact that the wood density of beech trees growing in Greece is generally larger than for northern European beeches [18]. Alternatively, one could speculate that Greek trees support a larger biomass at any given $D$ in comparison to Dutch and Spanish trees. Surprisingly, American regressions more accurately predicted raw data for the Greek forest than Spanish or Dutch equations, contrary to speculation that trees growing in similar environment may sustain quite similar aboveground biomass. Stand structural characteristics or anatomical parameters of the study trees may also play an important role on biomass production and allocation.

Finally, the theoretical model [30] did not perform so accurately for the Spanish and the pooled dataset. Chambers et al. [5] who compared several models for trees growing in the tropical zone also reported the same conclusion. Thus, the applicability of this theoretical model at the stand scale is questioned and the use of constant $a$ and $b$ values for trees growing in different environmental conditions should be viewed as tentative; more work is required to test whether this theoretical model may be used at the landscape scale.

### Acknowledgements

Christos Kontonasios and Thomas Zianis significantly contributed in collecting raw data. Dimitris Zianis is supported by Scholarship State Foundation of Greece (IKY) and Maurizio Mencuccini was supported by the EU-FUNDED CARBOAGE project (contract n. EVK2-CT-1999-00045).

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